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 A f , f 4 f @ @ @ f G f f @ - -  
 f @ f f f @ f

$$\begin{aligned}
 \mathbf{A}^N &= \mathbf{A}^W \left( \frac{\partial}{\partial \mathbf{f}} \right) \mathbf{A}^8 \mathbf{A}^1 \mathbf{U}^{\text{FF}} \mathbf{f} \\
 &= \delta \dots, \tag{4}
 \end{aligned}$$

$$\begin{aligned}
 \mathbf{F} &= \mathbf{f} \\
 \sigma &= 2\pi \omega \dots
 \end{aligned}$$

$$\begin{aligned}
 \mathbf{U} &= \mathbf{F} \left( \frac{\partial}{\partial \mathbf{f}} \right), \\
 &= \frac{\pi}{\tau} \int_{-\infty}^{\infty} \frac{\omega^2}{4} \omega, \\
 & \tag{3}
 \end{aligned}$$

$$G_{\tau} = \int_{-\infty}^{\infty} \frac{\pi}{\tau} \frac{\omega^2}{2\pi \omega} \dots \omega.$$

$$\begin{aligned}
 \mathbf{C} &= \left( \frac{\partial}{\partial \mathbf{f}} \right) \left( \frac{\partial}{\partial \mathbf{f}} \right) \mathbf{f} \left( \frac{\partial}{\partial \mathbf{f}} \right) \left( \frac{\partial}{\partial \mathbf{f}} \right) \frac{2\pi \omega}{\tau}, \\
 G_{\tau} &= \int_{-\infty}^{\infty} \frac{\pi}{\tau} \frac{\omega^2}{2\pi \omega} \dots \frac{\omega^2}{\tau} \frac{\omega}{\pi} \omega. \tag{8}
 \end{aligned}$$

$$\begin{aligned}
 \Gamma &= \mathbf{f} \mathbf{G} \mathbf{f} \left( \frac{\partial}{\partial \mathbf{f}} \right) \left( \frac{\partial}{\partial \mathbf{f}} \right) \tag{8} \\
 &= \mathbf{F} / \pi \epsilon, \tag{8} \\
 \omega &< \tau, \quad \epsilon / \pi, \quad \tau \leq \frac{1}{2}, \quad \mathbf{f}^{\hat{\xi}}
 \end{aligned}$$

$$\xi < \frac{\tau}{2\pi} \frac{\epsilon}{\pi}. \tag{9}$$

$$\begin{aligned}
 \mathbf{W} &= \mathbf{f} \lambda > \gamma_{\lambda} \tau \lambda^2, \quad \mathbf{F} \mathbf{f} \hat{\gamma} \xi, \quad \mathbf{L} \mathbf{G} \\
 &= \hat{\gamma}_{\lambda} \xi \tau^2, \quad \epsilon \in \mathbb{Z} \tag{4}
 \end{aligned}$$

$$\begin{aligned}
 \mathbf{U} &= \left( \frac{\partial}{\partial \mathbf{f}} \right) \mathbf{A} \left( \frac{\partial}{\partial \mathbf{f}} \right) \mathbf{3}, \quad \mathbf{f} \xi \leq \frac{N}{2} \\
 \hat{\xi} &\approx \frac{1}{\tau \lambda \frac{\xi}{vN}} \hat{\gamma}_{\lambda} v \xi, \tag{11}
 \end{aligned}$$

$$\mathbf{g}_n \left( \frac{\partial}{\partial \mathbf{f}} \right) \mathbf{A} \tag{26} \quad N \geq v \tag{11} \quad \mathbf{A} \tag{8} \quad \mathbf{A}^N \tag{N}$$

$$G_{\tau} \approx \tilde{G}_{\tau} = \int_{-\infty}^{\infty} \frac{\pi}{\tau} \frac{\omega^2}{2\pi \omega} \frac{\gamma_{\lambda} v \frac{\tau}{\pi} \omega}{\tau \lambda \frac{\tau / \pi \omega}{vN}}. \tag{12}$$

$$\begin{aligned}
 \mathbf{C} &= \left( \frac{\partial}{\partial \mathbf{f}} \right) \left( \frac{\partial}{\partial \mathbf{f}} \right) \left( \frac{\partial}{\partial \mathbf{f}} \right) \tag{12} \\
 \tilde{G}_{\tau} &= \int_{-\infty}^{\infty} \frac{\pi}{\tau} \frac{\omega^2}{2\pi \omega} \frac{\gamma_{\lambda} v \frac{\tau}{\pi} \omega}{\tau \lambda \frac{\tau / \pi \omega}{vN}} \omega. \tag{13}
 \end{aligned}$$

(13)  $\frac{1}{N} \int_{-\infty}^{\infty} \frac{\pi^2 \omega^2}{2\pi \omega} \lambda v^2 \frac{\omega}{\pi} \frac{\pi \omega^2}{v N^2 \lambda} \omega$

$$\times \frac{v N \lambda \pi}{\kappa} \times \frac{\lambda^2 v^2 N^2 \pi \omega^2 \lambda^2 \pi^2 \lambda v^2 N^2 \omega^2}{\kappa} \times 2 \frac{\pi^2 \lambda^2 v^4 N^2 \pi \lambda^2 v^3 N^2}{\kappa}$$

$$\kappa \pi^2 \lambda v^2 N^2 \pi^2 \lambda^2 v^4 N^2 \quad (14)$$

$\Gamma$

$$\tilde{G} = \frac{v N \lambda \pi}{\kappa} \frac{\pi^2 \lambda v^2 N^2 \omega^2 \lambda^2 \pi^2 \lambda v^4 N^2}{\kappa} \times \tilde{\Gamma} \frac{\lambda^2 v^2 N^2 \pi \omega^2}{\kappa} \frac{2 \pi \lambda^2 v^3 N^2}{\kappa}$$

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$$\tilde{\Gamma} = \frac{\lambda \pi^2 \omega^2}{\kappa} \quad (16)$$

$M$  (  $\mathbb{R}^n$  )  $\mathbb{W}$   $\mathbb{R}^n$ ,  $\frac{1}{2}$   $\mathbb{W}$   $\mathbb{R}^n$ ,  $\mathbb{R}^n$   $\frac{1}{2}, \frac{1}{2}$ ,  
 $\epsilon$ ,  $x$   $S_j$ ,  $f$   
 $\epsilon^2 \leq \epsilon$ ,

$$r \leq \frac{\epsilon}{\dots}$$

$\Gamma$   $f$ ,  $K$   $C_k$ ,  
 $s_{\frac{1}{2}, \frac{1}{2}} \epsilon^4$   $4$   $9$   $(M)$   $-$   $3$   $2$   $1$





$\Gamma$ ,  $\mathbb{Z}$ ,  $\hat{\gamma}_\lambda \xi$ ,  $\gamma_\lambda \xi$ ,  $f$ ,  $M$ ,  $\mathbb{A}$  .4



**A**  $f_{\xi}^{\nu}$ ,  $f_{\xi}^{\nu}$  **A 9)**  $\hat{\xi}$

$$\mathcal{P}^{\nu} = \int_{-\infty}^{\infty} 2\pi \xi^{\nu} \hat{v} N \xi \hat{\gamma}_{\lambda} \xi \xi, \quad \mathbf{A 10}$$

$$\mathcal{P}^{\nu} = \int_{-\frac{1}{2}}^{\frac{1}{2}} 2\pi \xi^{\nu} \hat{v} N \xi \hat{\gamma}_{\lambda} \xi \xi, \quad \mathbf{A 11}$$

$\mathbb{W}_{\xi}$   $\hat{\xi}$ ,  $\hat{\gamma}_{\lambda} \xi$  **A 10)** **A 11)**,  $f_{\xi}^{\nu}$ ,  $f_{\xi}^{\nu}$ ,  $f_{\xi}^{\nu}$

$$F_{\xi}^{\nu} = \int_{\mathbb{Z}} \mathcal{P}^{\nu} \xi^{2\pi} \xi, \quad \mathbf{A 12}$$

$$F_{\xi}^{\nu} = \int_{\mathbb{Z}} \hat{v} N \xi \hat{\gamma}_{\lambda} \xi \xi, \quad \mathbf{A 13}$$

$\hat{\xi}$   $\hat{\xi}$  **A 13)**,  $\hat{\xi}$   $\hat{\xi}$

Then

$$E_\infty \leq 1 - \hat{\varphi}(\alpha) \frac{1}{C^{-1/2, \alpha}}, \quad \alpha \in \mathbb{Z}, \quad \hat{\varphi}(\alpha) > 0, \quad \alpha > 0.$$

$$\hat{\varphi}(\alpha) = \sum_{l=1}^{\alpha} \frac{f_l}{1 + f_l}, \quad \alpha \in \mathbb{Z}, \quad f_l = \frac{1}{2} \left( \lambda + \sqrt{\lambda^2 - 4l} \right), \quad \lambda > 1, \quad f_l > 0, \quad l > 0.$$

For  $\lambda < 1$ ,  $\hat{\varphi}(\alpha) \leq 1$ ,  $\alpha \in \mathbb{Z}$ ,  $\alpha > 0$ . For  $\lambda > 1$ ,  $\hat{\varphi}(\alpha) > 1$ ,  $\alpha \in \mathbb{Z}$ ,  $\alpha > 0$ .

$$f_{16} = 1.6, \quad f_{23} = 1.6$$

$$A(9)$$

$$\lambda = 1.4$$

$$f_{33} = 1.6$$

$\frac{1}{2v}$

(2) C

$$F(\xi) = \int_{-\frac{vN}{2}}^{\frac{vN}{2}-1} \mathcal{P}^v e^{-2\pi i \xi t} dt$$

A 16

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(3)  $\rightarrow F(\xi_j) = \dots, \lambda \xi$

### A.2.2. Fast evaluation of the Fourier series at unequally spaced points

$$L = \int_{-\frac{vN}{2}}^{\frac{vN}{2}-1} f(t) e^{-2\pi i \xi t} dt, \quad \text{where } \xi = \frac{k}{T}$$

$$\xi = \frac{F(\xi/v)}{\dots, \lambda \xi/v}$$

$F(\xi) = \dots$  A 12)  $a_\lambda(\xi)$  A 4) C

$$\hat{f}(\xi) = \int_{-\infty}^{\infty} f(t) e^{-2\pi i \xi t} dt$$

$$f(\xi) = \sum_{\nu=-\infty}^{\infty} \hat{G} \frac{\xi}{\nu} \tilde{\mathcal{P}}^{\nu}(\xi) \quad \text{A .20}$$

$$\hat{G} \frac{\xi}{\nu} = \frac{1}{\nu} \frac{e^{-i \frac{\nu \xi}{vN}}}{1 + i \frac{\nu \xi}{vN}} \quad \text{A .21}$$

Using (19) and (20),

$$f(\xi) = \sum_{\nu \in \mathbb{Z}} \hat{G} \frac{\xi}{\nu} \gamma_{\lambda} v N \tilde{\mathcal{P}}^{\nu}(\xi) = \sum_{\nu \in \mathbb{Z}} \hat{G} \frac{\xi}{\nu} \gamma_{\lambda} v N \tilde{\mathcal{P}}^{\nu}(\xi) \quad \text{A .22}$$

$$\tilde{\mathcal{P}}^{\nu}(\xi) = \hat{G} \frac{\xi}{\nu} \gamma_{\lambda} v \xi \quad \text{A .23}$$

For  $\nu \in \mathbb{Z}$ ,  $\tilde{\mathcal{P}}^{\nu}(\xi) = \frac{1}{\nu} \Gamma(\frac{\nu \xi}{vN})$ ,  $\frac{N}{2} \leq \nu \leq \frac{N}{2} - 1$ ;

$$\tilde{\mathcal{P}}^{\nu}(\xi) = \frac{1}{\nu} \Gamma(\frac{\nu \xi}{vN}) \quad \text{A .24}$$

Algorithm 2.  $\tilde{\mathcal{P}}^{\nu}(\xi) = \frac{1}{\nu} \Gamma(\frac{\nu \xi}{vN})$ ,  $\tilde{\mathcal{P}}^{\nu}(\xi) = \frac{1}{\nu} \Gamma(\frac{\nu \xi}{vN})$ ,  $\tilde{\mathcal{P}}^{\nu}(\xi) = \frac{1}{\nu} \Gamma(\frac{\nu \xi}{vN})$

Algorithm 2.

- (1) C  $\tilde{\mathcal{P}}^{\nu}(\xi) = \frac{1}{\nu} \Gamma(\frac{\nu \xi}{vN})$  (A .24)
- (2) A FFT  $\tilde{\mathcal{P}}^{\nu}(\xi) = \frac{1}{\nu} \Gamma(\frac{\nu \xi}{vN})$
- (3) C  $\tilde{\mathcal{P}}^{\nu}(\xi) = \frac{1}{\nu} \Gamma(\frac{\nu \xi}{vN})$  (A .23)

A.2.3. Evaluation of unequally spaced FFT at unequally spaced points

$$f(\xi) = \sum_{\nu \in \mathbb{Z}} \hat{G} \frac{\xi}{\nu} \gamma_{\lambda} v N \tilde{\mathcal{P}}^{\nu}(\xi) \quad \text{A .14),}$$

Algorithm 3.

- (1) C  $\tilde{\mathcal{P}}^{\nu}(\xi) = \frac{1}{\nu} \Gamma(\frac{\nu \xi}{vN})$ ,  $\frac{v^2 N}{2}, \dots, \frac{v^2 N}{2} - 1$  (A .2)
- (2) A  $\tilde{\mathcal{P}}^{\nu}(\xi) = \frac{1}{\nu} \Gamma(\frac{\nu \xi}{vN})$ ,  $\tilde{\mathcal{P}}^{\nu}(\xi) = \frac{1}{\nu} \Gamma(\frac{\nu \xi}{vN})$

