

4. (20 points) Consider the function $g(x) = \frac{2x^2 - 12x + 16}{x^2 - 7x + 12}$.

(Reminder: You may not use L'Hôpital's Rule or "Dominance of Powers" in any solutions on this exam.)

- (a) Find the domain of $g(x)$. Express your answer in interval notation.
- (b) Find and classify all discontinuities of $g(x)$; justify your answers by calculating the appropriate limits.
- (c) Find the horizontal asymptotes, if any; justify your answers by calculating the appropriate limits.

5. (10 points) Consider the function

$$f(x) = \begin{cases} b \cos(x); & x < 1 \\ \frac{2x - 2}{3}; & x > 1 \end{cases}$$

Find the value of b such that $\lim_{x \rightarrow 1} f(x)$ exists. Justify your answer by calculating appropriate limits.

6. (10 points) Show that the equation $x^2 = \sin x \cos x$ has at least one real solution. Indicate the interval where a solution can be found.