

Spatially structured oscillations in a two-dimensional excitatory neuronal network with synaptic depression

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Abstract

Excitatory neuronal networks with synaptic depression can exhibit spatially structured oscillations. We study the dynamics of a two-dimensional excitatory neuronal network with synaptic depression. The network is modeled by a set of coupled differential equations. We show that the network exhibits spatially structured oscillations. The oscillations are characterized by a spatial pattern of activity that oscillates in time. The spatial pattern is determined by the network parameters and the initial conditions. The oscillations are observed in both *in vivo* and *in vitro* experiments. The oscillations are characterized by a spatial pattern of activity that oscillates in time. The spatial pattern is determined by the network parameters and the initial conditions. The oscillations are observed in both *in vivo* and *in vitro* experiments.

Keywords

Spatially structured oscillations, synaptic depression, neuronal network, two-dimensional, excitatory, synaptic depression, spatially structured oscillations, neuronal network, two-dimensional, excitatory, synaptic depression.

1 Introduction

Spatially structured oscillations in a two-dimensional excitatory neuronal network with synaptic depression. We study the dynamics of a two-dimensional excitatory neuronal network with synaptic depression. The network is modeled by a set of coupled differential equations. We show that the network exhibits spatially structured oscillations. The oscillations are characterized by a spatial pattern of activity that oscillates in time. The spatial pattern is determined by the network parameters and the initial conditions. The oscillations are observed in both *in vivo* and *in vitro* experiments. The oscillations are characterized by a spatial pattern of activity that oscillates in time. The spatial pattern is determined by the network parameters and the initial conditions. The oscillations are observed in both *in vivo* and *in vitro* experiments.

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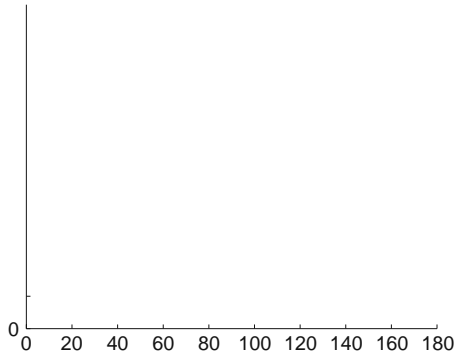
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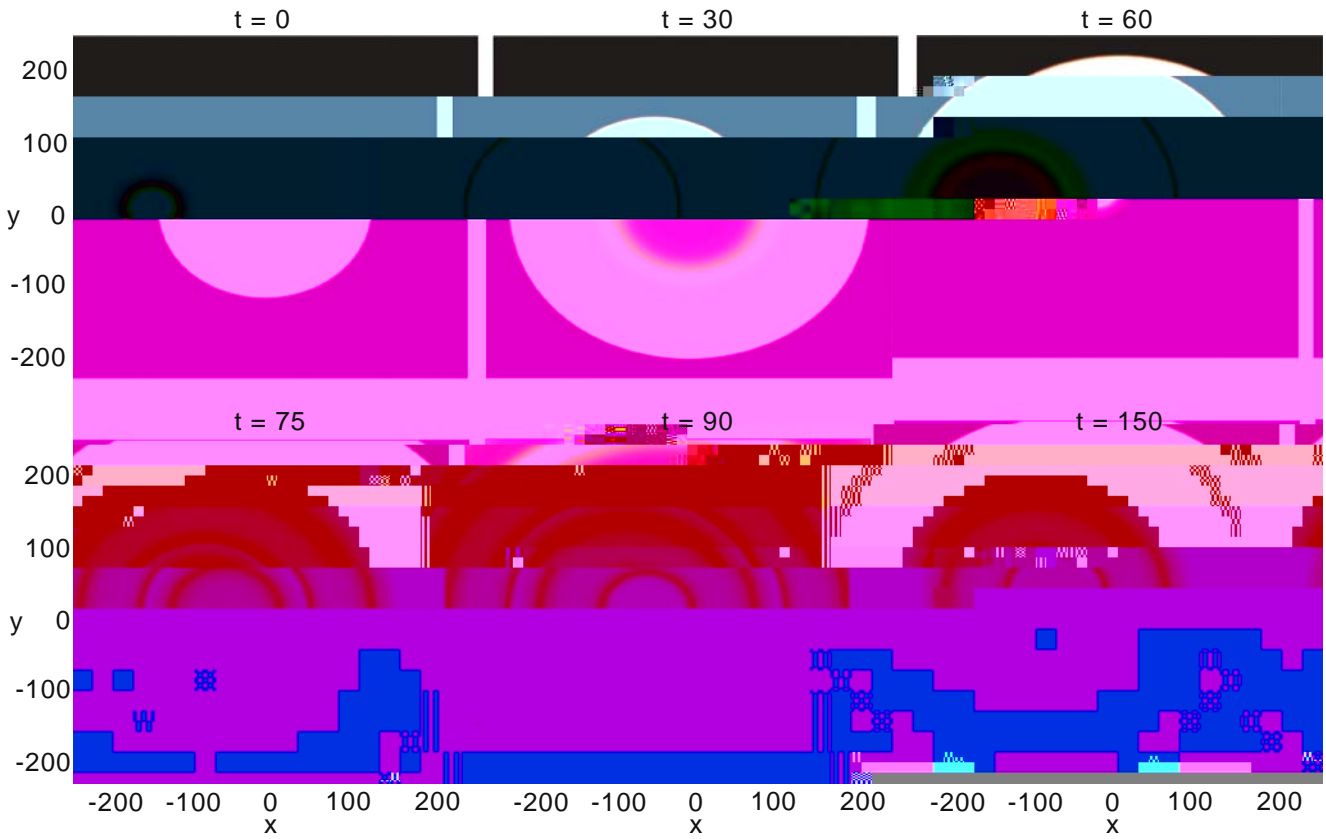


Fig. 7 Snapshots of the evolution of the system at different times t . The snapshots are arranged in two rows of three. The vertical axis is labeled y and ranges from -200 to 200 . The horizontal axis is labeled x and ranges from -200 to 200 . The snapshots show a progression of a wave-like pattern moving and changing shape over time.

The snapshots show a progression of a wave-like pattern moving and changing shape over time. The snapshots are arranged in two rows of three. The vertical axis is labeled y and ranges from -200 to 200 . The horizontal axis is labeled x and ranges from -200 to 200 .

At $t=0$, the system is in a state where the top and bottom regions are dark. As time progresses, these regions interact and form more complex, multi-colored patterns (pink, red, blue, green). The snapshots show a progression of a wave-like pattern moving and changing shape over time.

The snapshots show a progression of a wave-like pattern moving and changing shape over time. The snapshots are arranged in two rows of three. The vertical axis is labeled y and ranges from -200 to 200 . The horizontal axis is labeled x and ranges from -200 to 200 .

$$L_h \frac{u_{ij}^{k+} - u_{ij}^k}{t} + u_{ij}^{k+} = M q_{ij} f, u_{ij} \quad (.1)$$

$$L_h \frac{q_{ij}^{k+} - q_{ij}^k}{t} = - q_{ij} f, u_{ij} \quad (.)$$

$i = 1, \dots, N_x, j = 1, \dots, N_y, L_h \neq t$
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 $u_{ij} = q_{ij} f, u_{ij} \quad (.1),$

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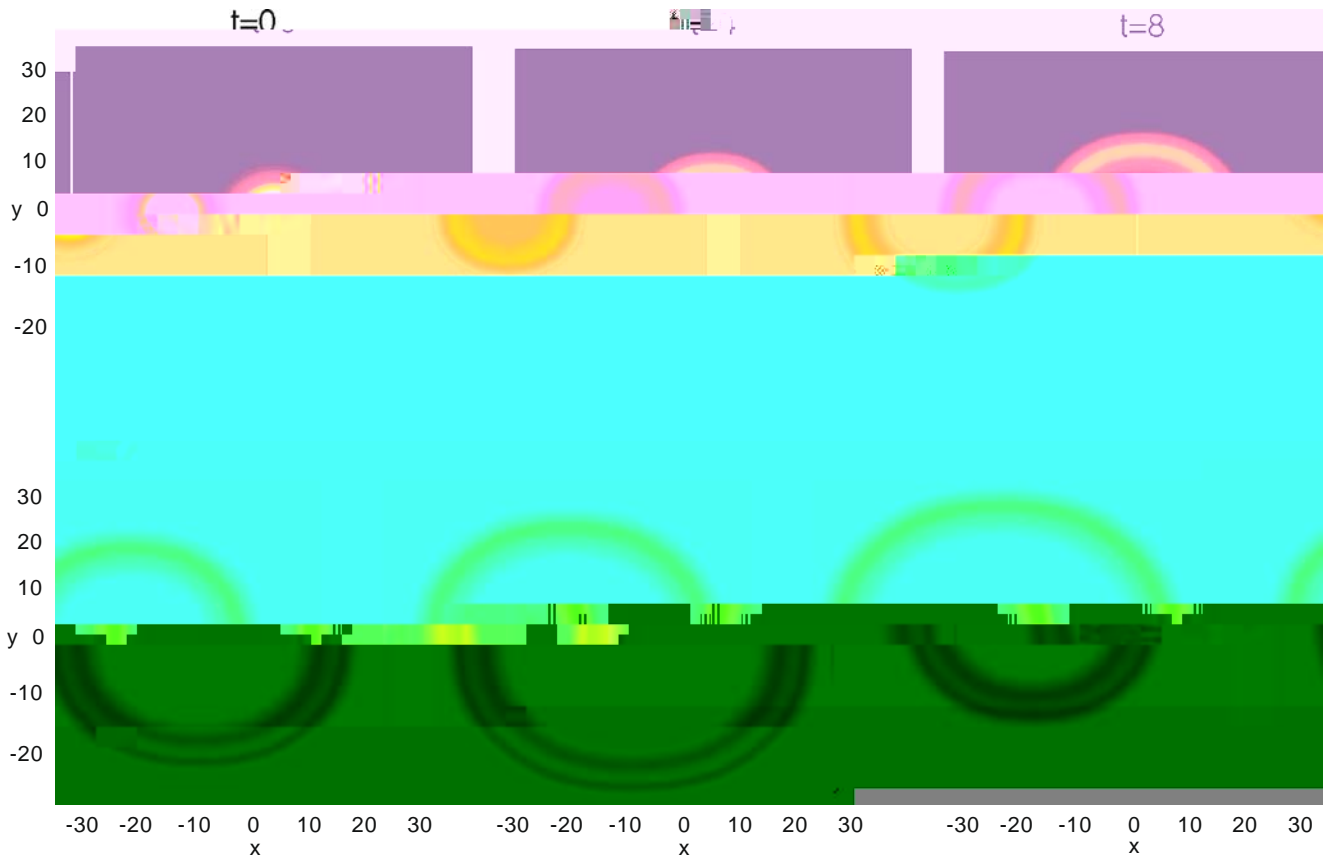


Fig. 13 S_i t_j u(x, y)

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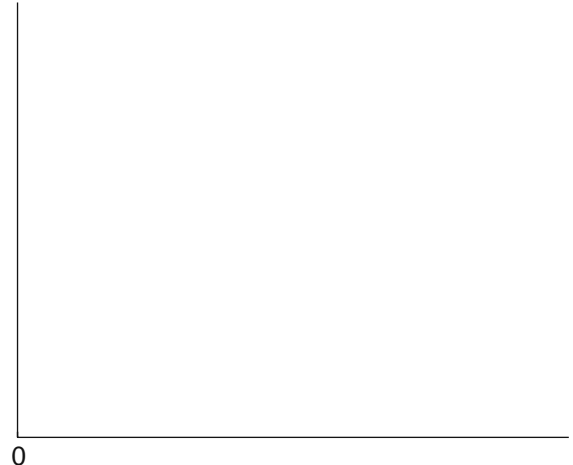
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Acknowledgements

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